## SM339 - Applied Statistics • Spring 2024 - Uhan

## Quiz 1-1/18/2024

## Instructions

This take-home quiz is due on Thursday, January 18 at 23:59.
You may use your own course materials, as well as any materials directly linked from the course website. No collaboration allowed.

Type your answers directly in this Jupyter notebook, and submit this notebook (just the ipynb file) using the submission form on the course website.

## Problem 1

Suppose $X$ has a $t$-distribution with 13 degrees of freedom.
Write R code to compute the following.
a.
$P(X \leq 0.64)$

In [ ]:
b.
$P(X>-0.12)$

In [ ]:
C.
$P(0.17<X \leq 0.43)$

In [ ]:
d.

The 0.85 -quantile of $X$.

In [ ]:

Feedback. Most of you had the right idea with this problem.

Some things to remember about pt() vs qt() in R. Assume $X$ has a $t$-distribution with $d$ degrees of freedom:

1. $\mathrm{pt}(\mathrm{x}, \mathrm{df}=\mathrm{d})=P(X \leq x)$. See Problem 4 in the Lesson 2 Exercises.
2. $\mathrm{qt}(\mathrm{p}, \mathrm{df}=\mathrm{d})=$ the value of $x$ such that $P(X \leq x)=p$, or in other words, the $p$-quantile. See Problem 1 in the Lesson 2 Exercises.
3. For part b, note that $P(X>-0.12)=1-P(X \leq-0.12)$. You can compute $P(X \leq-0.12)$ using pt () ; see item 1 above.

## Problem 2

In the same folder as this notebook, there is a CSV file data/HumanTemp. Csv, with three columns/variables: Temp, Sex, and Pulse.

Write R code to do the following.
a.

Find the average of the values in Temp . (Read the data first!)
In [ ]:
b.

Compute the 1st quartile of the values in Temp. Do not use summary ().

In [ ]:
C.

Create a normal QQ-plot of the values in Temp .

In [ ]:
d.

Based on your answer to part c, do the values in Temp approximately follow a normal distribution? Explain.
Your explanation should be in complete sentences, with correct spelling and grammar. Some tips:

- Be specific. For example, if you use pronouns like "it" or "they", make sure you are clear about what those pronouns refer to.
- Be concise. Don't make your explanation longer than necessary. You can answer this question using only one or two sentences.

Write your answer here. Double-click to edit.

Feedback. Most of you had the right idea with parts a-c. For a similar problem, see Problem 5 in the Lesson 2
Exercises.

For part d: see the Normal Q-Q plot section in Lesson 2. Also, make sure your explanation is precise: use the correct words. In addition, keep your language simple. Some tips:

- Be specific. For example, consider the following sentence:

It follows a Normal distribution because it roughly is a straight line.

What does "it" refer to here? The first "it" refers to the values in Temp, and the second "it" refers to the Normal Q-Q plot.

- The Normal Q-Q plot consists of points, not values. You can say:

The points in the Normal Q-Q plot do not approximately follow a straight line.

You can also say:
The Normal Q-Q plot is not an approximately straight line.
But you should not say:
The values do not follow a straight line.

- You should be able to answer this problem using the following template:

The values in Temp (do or do not) approximately follow a Normal distribution because the points in the Normal Q-Q plot (fill in the blank here).

## Grading rubric

| Problem | Weight |
| :---: | :---: |
| 1a | 1 |
| 1b | 1 |
| 1c | 1 |
| 1d | 1 |
| 2a | 1 |
| 2b | 1 |
| 2c | 1 |
| 2d | 1 |
| Max Score | 80 |

